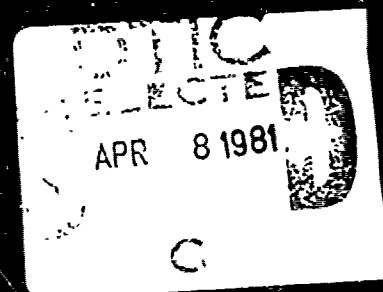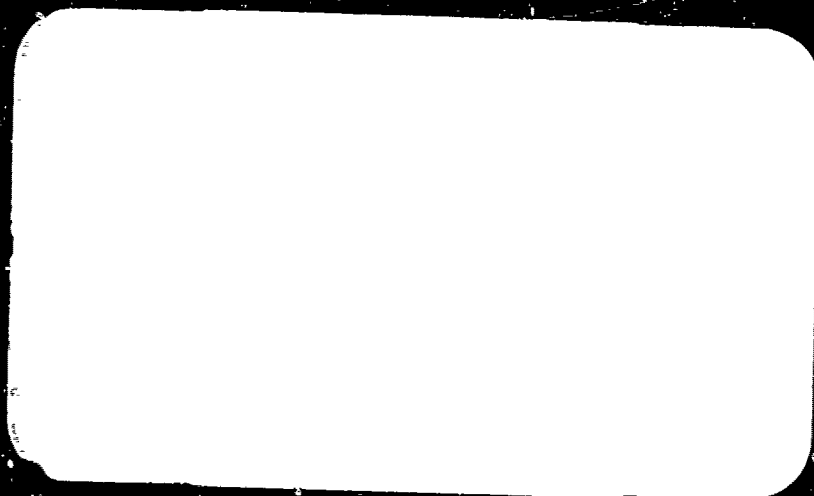# A DIFFERENCE IN EFFICIENCY

BETWEEN SYNCHRONOUS AND ASYNCHRONOUS SYSTEMS*

by

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A system of parallel processes is said to be synchronous if all processes run using the same clock, and it is asynchronous if each process has its own independent clock. For any s, n, a particular distributed problem is defined involving system behavior in n "ports". This problem can be solved in time s by a synchronous system but requires time at least $(s-1) \log n$ on any asynchronous system.

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A DIFFERENCE IN EFFICIENCY BETWEEN SYNCHRONOUS AND ASYNCHRONOUS SYSTEMS*

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ABSTRACT

A system of parallel processes is said to be
asynchronous if all processes run using the same
clock, and it is asynchronous if each process has
its own independent clock. For any s, n, a par-
ticular distributed problem is defined involving
system behavior at n "ports". This problem can be
solved in time s by a synchronous system but re-
quires time at least (s-1) log n on any asynchro-
nous system.

INTRODUCTION

A system of parallel processes is said to be
synchronous if all processes run using the same
clock, so the processes operate in lock-step, and
it is asynchronous if each process has its own in-
dependent clock. Examples of synchronous systems
are large centralized multiprocessing computers
and VLSI chips containing many separate parallel
processing elements. Examples of asynchronous sys-
tems are distributed computer networks and I/O
systems for conventional computers.

In this paper, we compare time efficiency of
a simple model of a synchronous system with a
similar asynchronous model. We bound the number
of processes that can access any particular com-
munication channel, and that restriction is crucial
to our results. For s, n ε N, we define a partic-
ular distributed problem involving n "ports". It
can be solved in time s on a synchronous system
but we show it requires time at least $(s-1) \lfloor \log_b n \rfloor$
on any asynchronous system. Here b is a constant

reflecting the communication bound in the model,
whose precise definition is given in the next
section. If we strengthen the communication sys-
tem slightly to permit a single designated process
to broadcast to all the others, or if we provide
each process with access to a global clock, then
the asynchronous model can solve the problem in
time $O(s)$.

THE MODELS

We use a version of the model of a concurrent
system defined in [LF79,LF81]. Briefly, it con-
sists of collections P of processes and X of
shared variables. The global state of the system
consists of the internal state of each process to-
gether with the value of each shared variable. A
step is an atomic action which consists of simul-
taneous changes to the state of some process and
the value of some shared variable. Formally, a
step σ is a pair of triples $((s,p,t),(u,x,v))$
where s, t are possible internal states of process
p, and u, v are possible values of variable x. We
define process(σ) = p and variable(σ) = x and say
σ involves p and accesses x. Step σ is applicable
to any global state in which process p has inter-
nal state s and variable x contains value u. The
effect of performing σ is to change the state of
p to t and simultaneously to change the value of
x to v.

A system is specified by describing P, X, an
initial global state, and a set OKSTEPS of possi-
ble steps. A process p blocks in a global state
g if there is no step σ in OKSTEPS applicable to g
with process(σ) = p. In this paper, we require
our systems to be non-blocking for all processes
and all global states.

Let x ε X and define locality(x) =
{process(σ) : σ ε OKSTEPS and variable(σ) = x}. A
system is b-bounded if |locality(x)| ≤ b for every
x ε X.

A computation of a system is a finite or in-
finite sequence of steps in OKSTEPS such that the
first step is applicable to the initial global
state, and each succeeding step is applicable to
the state resulting from the application of the
previous step. The result of a finite computation
is the global state after applying the sequence.
An infinite computation is admissible if every
process appears in infinitely many steps of the

---

sequence.

A round is any sequence of steps such that every process appears at least once in the sequence. A minimal round is a round such that no proper prefix is a round. Every sequence of steps can be uniquely partitioned into segments such that every segment is a round, except possibly for the last if the sequence is finite, and every round is minimal. We call this a partition into minimal rounds, even though the last segment is not necessarily a round.

A sequence of steps is synchronous if in the unique partition into minimal rounds:

(1) No two steps in the same round involve the same process;

(2) No two steps in the same round access the same variable.

(1) and (2) together imply that the steps in each round are independent and can be performed in any order, or simultaneously, with the same result.

The run time for a finite sequence of steps is defined to be the number of segments in the partition into minimal rounds. (This definition is equivalent to the one in [LF81] which says it is the longest amount of elapsed real time that the system could take to execute the sequence, subject to the constraint that the time delay between two steps of the same process is at most unity. For synchronous systems, this definition is also equivalent to the more usual one which simply counts the number of synchronous steps of the system, where one synchronous step consists of the simultaneous execution of a step by each process.)

Finally, a synchronous system is a concurrent system whose allowable computations are all of its infinite synchronous computations. An asynchronous system is a concurrent system whose allowable computations are all of its infinite admissible computations.

THE PROBLEM

We now define a particular behavior for a concurrent system. Let $Y \subseteq X$ be a distinguished set of variables called ports. A port event is any step that accesses a port. A session is any sequence of steps containing at least one port event for every port. A computation performs s sessions if it can be partitioned into s segments, each of which is a session. An infinite computation is ultimately quiescent if it contains only a finite number of port events. The time to quiescence of an ultimately quiescent sequence is the run time of the shortest prefix containing all port events.

Let $s, n \in \mathbb{N}$. The (s,n)-session problem is the problem of finding a concurrent system with n ports such that every allowable computation performs (at least) s sessions and is ultimately quiescent.

Note that the (s,n)-session problem, like the mutual exclusion and dining philosophers

problems, concerns possible orderings of sequences of events rather than the computation of particular outputs. It is an abstraction of the synchronization needed in many natural problems. Consider, for example, a simple message distribution system in which a sending process writes a sequence of s messages one at a time on a board visible to all and waits after each message until all n other processes have read the message. Whatever protocol insures that the sender has waited sufficiently long will also solve the (s,n)-session problem.

MAIN RESULT

We show that any asynchronous b-bounded system solving the (s,n)-session problem requires time at least $(s-1) \lfloor \log_b n \rfloor$ to quiescence, whereas there is a trivial synchronous system which solves the problem in time exactly s. This is the first example we know of, of a problem for which an asynchronous system is provably slower than a synchronous one, and it shows that a straightforward step-by-step and process-by-process simulation of an n-process synchronous system by an n-process asynchronous one necessarily loses a factor of $\log_b n$ in speed.

The result is even more surprising when one realizes that the trivial asynchronous system with one process per port (and no communication among the processes) in which each process does nothing except access a port on each step in fact performs s sessions within time s. The difficulty is that no process knows when time s has elapsed (due to the lack of a global system "clock"), nor does it know when the s sessions have in fact been achieved, so none of the processes knows when to stop accessing its port.

A procedure which does work is for a process associated with each port to perform a port event, broadcast that fact and then wait until it has heard that all other port processes have performed their port events and that the session has been completed. This is repeated s times. By making the port processes the leaves of a tree network, the necessary communication for one session can be accomplished in time $O(\log n)$; hence, the total time to quiescence for the solution is $O(s \log n)$. It seems very inefficient to wait after each port event, and one might try to invent clever schemes to increase the concurrency in the system. Our lower bound shows, however, that this method is optimal to within a constant factor, so only a limited amount of improvement is possible.

We now present the formal results.

Theorem 1. For all $s, n \in \mathbb{N}$, there is a 1-bounded synchronous system which solves the (s,n)-session problem, such that the time to quiescence for each allowable computation is s.

Proof. The system has n processes, one corresponding to each port. Each process accesses its port on each of its first s steps and then ceases performing port events. In every infinite synchronous computation, each of the first s minimal rounds constitutes a session,

and the system becomes quiescent after s rounds. Hence, the system solves the (s,n)-session problem in time s. ☐

Theorem 2 (Main Result). Assume $b, s, n \in \mathbb{N}$, $b \geq 2$. For every b-bounded asynchronous system which solves the (s,n)-session problem, the time to quiescence is at least $(s-1) \lfloor \log_b n \rfloor$ for some allowable computation.

The proof of Theorem 2 involves a series of three lemmas about a particular partial ordering of steps of a computation. (The ordering represents a kind of logical dependency.) We break up the proof of Theorem 2 by presenting the lemmas before the main proof. These lemmas and their proofs are self-contained and depend only on the properties given below. For better intuitive motivation, however, the reader may wish to read the main proof before reading the lemmas.

Let R be the set $\{1,\ldots,s\}$ (of "round" numbers), P a finite set (of "processes"), X a set (of "variables"). Let D be a set having mappings round : $D \to R$, proc : $D \to P$ and var : $D \to X$. Assume that for every pair $(r,p) \in R \times P$, there is exactly one $\sigma \in D$ having round$(\sigma) = r$ and proc$(\sigma) = p$. Let loc$(x) = \{$proc$(\sigma) : \sigma \in D$ and var$(\sigma) = x\}$. Let $b \geq 2$ and assume $|$loc$(x)| \leq b$ for all $x \in X$.

Let $\leq$ be a partial order on D, and write $\sigma \leq_1 \tau$ to indicate that $\sigma < \tau$ and there is no ρ with $\sigma < \rho < \tau$. Assume that $\leq$ has the following properties:

(i) If $\sigma \leq_1 \tau$, then either var$(\sigma) = $ var(τ) or proc$(\sigma) = $ proc(τ).

(ii) If either var$(\sigma) = $ var(τ) or proc$(\sigma) = $ proc(τ), then σ and τ are $\leq$-comparable.

(iii) If $\sigma \leq \tau$, then round$(\sigma) \leq $ round(τ).

Finally, let dep$(\sigma) = \{$var$(\tau) : \sigma \leq \tau\}$.

Lemma 1 (Monotonicity). If $\sigma_1 \leq \sigma_2$, then dep$(\sigma_2) \subseteq $ dep(σ_1).

Proof. Obvious from the definition of dep. ☐

Lemma 2. Let $\sigma \in D$, round$(\sigma) = r$, var$(\sigma) = x$. Let $C = \{\tau \in D : $ round$(\tau) = r + 1$ and proc$(\tau) \in $ loc$(x)\}$.

Then dep$(\sigma) \subseteq \bigcup_{\tau \in C} $ dep$(\tau) \cup \{x\}$.

Proof. Proof is by induction on $\leq$, beginning with maximal elements. Let $\sigma \in D$ and assume the lemma holds for all $\tau > \sigma$. Assume r, x and C are defined from σ as in the statement of the lemma. If there exists $\sigma' \in D$ with var$(\sigma') = x$ and $\sigma' > \sigma$, then fix σ' as the smallest such member of D. (Property (ii) insures that σ', if it exists, is defined uniquely.) Similarly, if there exists $\sigma'' \in D$ with proc$(\sigma'') = $ proc(σ) and $\sigma'' > \sigma$, then

fix σ'' as the smallest such member of D. Define $B' = $ dep(σ') if σ' exists, ϕ otherwise, and $B'' = $ dep(σ'') if σ'' exists, ϕ otherwise. Then properties (i) and (ii) and monotonicity show that dep$(\sigma) \subseteq B' \cup B'' \cup \{x\}$. It suffices to show that $B' \cup B'' \subseteq \bigcup_{\tau \in C} $ dep$(\tau) \cup \{x\}$.

We first consider B', and assume σ' exists. (If σ' does not exist, there is nothing to prove.) By induction, $B' \subseteq \bigcup_{\tau \in C'} $ dep$(\tau) \cup \{x\}$, where $C' = \{\tau \in D : $ round$(\tau) = $ round$(\sigma') + 1$ and proc$(\tau) \in $ loc$(x)\}$. For every $\tau' \in C'$, there exists $\tau \in C$ with proc$(\tau) = $ proc(τ'). Property (ii) shows that τ and τ' are $\leq$-comparable; property (iii) shows that $\tau \leq \tau'$. Monotonicity implies that dep$(\tau') \subseteq $ dep(τ). Thus,

$B' \subseteq \bigcup_{\tau \in C} $ dep$(\tau) \cup \{x\}$, as needed.

Finally, we consider B'', and assume σ'' exists. Then the properties of D and $\leq$ show that round$(\sigma'') = r + 1$, so that $\sigma'' \in C$.

Thus, $B'' \subseteq \bigcup_{\tau \in C} $ dep(τ), as needed. ☐

Lemma 3. For each $\sigma \in D$, it is the case that

$$|\text{dep}(\sigma)| \leq \frac{b^{s-\text{round}(\sigma)+1} - 1}{b-1}.$$

Proof. We proceed by induction on $k = $ round(σ), starting with $k = s$ and working backwards.

BASIS: $k = s$. By Lemma 2, dep$(\sigma) \subseteq \{$var$(\sigma)\}$, so $|$dep$(\sigma)| \leq 1$, as needed.

INDUCTION: $1 \leq k < s$. By Lemma 2, we have

$|$dep$(\sigma)| \leq \sum_{\tau \in C} |dep(\tau)| + 1$, where C is defined as in Lemma 2. Each $\tau \in C$ has round$(\tau) = k + 1$, so by induction, $|$dep$(\tau)| \leq \frac{b^{s-k} - 1}{b-1}$. Also, $|C| \leq b$. Hence, $|$dep$(\sigma)| \leq$

$$b \cdot \left[\frac{b^{s-k} - 1}{b-1} \right] + 1 = \frac{b^{s-k+1} - 1}{b-1}, \text{ as needed.}$$

☐

Proof of Theorem 2. Assume an asynchronous system which solves the (s,n)-session problem. Enumerate the processes arbitrarily. Construct an infinite admissible computation α by running the processes in round-robin order (one step of process 1, one of process 2,..., one step of process q, one step of process 1,...). Each round-robin round is minimal and contains exactly one step of each process; hence, the time to

perform the first r rounds is exactly r. Because
we assume a correct solution, this computation is
ultimately quiescent. Let t be the time to qui-
escence for this computation. Then round t is the
last round at which any port event occurs. We wish
to show $t \geq (s-1) \lfloor \log_b n \rfloor$.

Let $\alpha = \beta\gamma$, where β contains the first t
rounds of α, and γ is the remaining tail. Our
strategy is to construct a new infinite admissible
computation $\alpha' = \beta'\gamma$, where β' is a reordering of
the steps of β that results in the same global
state as β, but β' performs at most $t/\lfloor \log_b n \rfloor + 1$
sessions. Since no port events occur in γ, it
follows that α' performs at most $t/\lfloor \log_b n \rfloor + 1$
sessions. Since α' is an infinite admissible com-
putation for the system, $t/\lfloor \log_b n \rfloor + 1 \geq s$ and our
result follows.

To construct β', we first construct a partial
order of the steps in β, representing "dependency".
(Formally, the domain of the partial order consists
of ordered pairs (i, ξ_i), where ξ_i is the ith step
of β.) For every pair of steps σ, τ in β, we let
$\sigma \leq_\beta \tau$ if σ precedes τ in β and either process(σ) =
process(τ) or variable(σ) = variable(τ). Close $\leq_\beta$
under transitivity. $\leq_\beta$ is a partial order, and
every total order of the steps of β consistent
with $\leq_\beta$ is a computation which leaves the system in
the same global state as β. (Clearly β itself
defines such a total ordering.)

Now, let $m = \lceil t/\lfloor \log_b n \rfloor \rceil$, and write
$\beta = \beta_1 \ldots \beta_m$, where β_k consists of $\lfloor \log_b n \rfloor$ minimal
rounds, $1 \leq k < m$. Let y_0 be an arbitrary port.
For $k = 1, \ldots, m$, we define inductively a port y_k
and two sequences of steps ϕ_k and ψ_k, as follows.
There are two cases. First, if there is some port
which is not accessed by any step of β_k, then take
y_k to be that port and let $\phi_k = \Lambda$ (the null
sequence) and $\psi_k = \beta_k$. Otherwise, let τ_k be the
first step in β_k which accesses y_{k-1}. We now wish

to apply Lemma 3, to the suborderings of $\leq_\beta$ defined
by restriction to rounds with numbers
$(k-1)\lfloor \log_b n \rfloor + 1, \ldots, k\lfloor \log_b n \rfloor$ inclusive. The
mapping "rounds" required for the lemmas is ob-
tained by renumbering the rounds in the same order.
Mappings "proc" and "var" are obtained from the
mappings "process" and "variable" respectively.
It is straightforward to see that the necessary
properties of D and $\leq$ are satisfied. Then by
Lemma 3, we see that $|dep(\tau_k)| \leq$

$$ b^{\frac{\lfloor \log_b n \rfloor - 1 + 1}{}} \frac{-1}{b-1} \leq n - 1. $$ Since there are n ports,

this means that there must exist a port y_k
and a step σ_k such that

(i) σ_k is the last step in β_k which accesses
y_k;

(ii) it is false that $\tau_k \leq_\beta \sigma_k$.

Thus, adding the relation $\sigma_k \leq_\beta \tau_k$ to $\leq_\beta$ and
closing under transitivity results in another
partial order $\leq_k$. Choose any total ordering of
the steps in β_k consistent with $\leq_k$. Let ϕ_k be
the longest prefix of that ordering not contain-
ing any step accessing y_{k-1}, and let ψ_k be the
remainder. This is illustrated in Figure 1.

In either case, ϕ_k does not contain any
step which accesses y_{k-1} and ψ_k does not contain
any step which accesses y_k.

Let $\beta' = \phi_1\psi_1\phi_2\psi_2\ldots\phi_m\psi_m$. β' is consistent
with $\leq_\beta$, but β' contains at most $m \leq t/\lfloor \log_b n \rfloor + 1$
sessions, since each session must contain steps
on both sides of some ϕ_k-ψ_k boundary. (If a
sequence of steps were completely contained in
$\psi_{k-1}\phi_k$, for example, then it would fail
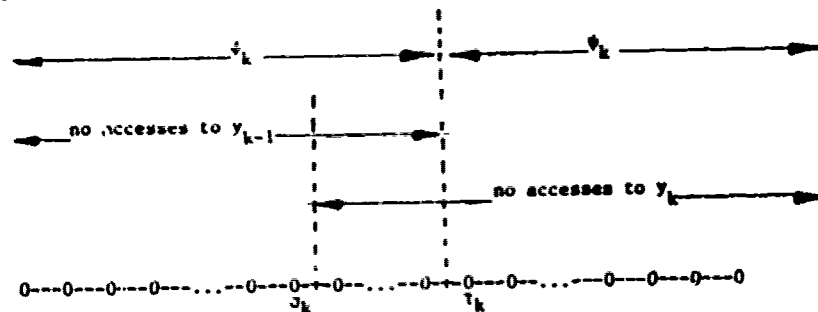to contain a step accessing port y_{k-1}.) □

Figure 1. A total ordering of steps in β_k consistent with $\leq_k$.

RESULTS FOR MORE GENERAL MODELS

If the model is generalized by removing the bound on the number of processes which can access a shared variable, then a single communication variable shared by n port processes can be used to construct an easy $O(s)$ solution.

In fact, if the original model is only generalized slightly by allowing one of the shared variables to be read by an arbitrary number of processes (but only to be changed by one process), then an $O(s + \log n)$ solution is possible. In more detail, we use a shared variable, the message board, which every process can read but only one fixed process, the supervisor, can change. Each port has a corresponding port process, and there are additional communication processes whose job it is to pass messages through a tree network from the port processes back to the supervisor. The message board contains an integer which we call a "clock" value. The supervisor alternately increments the clock and reads the messages being sent back. Each port process repeatedly performs a cycle of reading the clock, performing a port event, and sending a message back to the supervisor, through the network, which contains the clock value just read and the port identifier.

If c_1 and c_2 are two successive clock values sent by port process i, then a port event must occur at port i sometime after the clock assumes value c_1 and before the clock assumes value $c_2 + 1$. By naturally combining this information about all ports, the supervisor can construct a sequence $0 = b_0 < b_1 < b_2 < \ldots < b_s$ such that for each j, a session is guaranteed to occur between the times when the clock first assumes values b_j and b_{j+1}. (Specifically, let $c_{i1}, c_{i2}, \ldots$ denote the successive clock values sent by port process i, $1 \leq i \leq n$. Then define

$$b_j = \max \{c_{i(k+1)} + 1 : 1 \leq i \leq n \text{ and } k \text{ is the smallest index such that } c_{ik} \geq b_{j-1}\}, \text{ for each } j,$$

$1 \leq j \leq s$.) After the supervisor constructs this entire sequence, it knows that at least s sessions have in fact occurred, at which time it puts a "STOP" message on its message board. When the port processes read the "STOP" message, they stop performing port events.

It is easy to see that this construction solves the (s,n)-session problem. We argue that it satisfies the required $O(s + \log n)$ time bound.

First, we consider message transmission time. Since we are not assuming any upper bound on size of variables, the tree network can guarantee (by concatenating messages) that any message can be sent as soon as a process is ready to send it, and also that any message sent by time t is received by the supervisor by time $t + O(\log n)$.

Next, we claim that for each j, $1 \leq j \leq s$, the elapsed time between when the clock first

assumes values b_{j-1} and b_j is bounded above by a constant. For, from the time when the clock first assumes value b_{j-1}, it is at most a fixed constant amount of time before all port processes have read the clock, performed port events, sent messages containing clock values $\geq b_{j-1}$, and read the clock once again. Thereafter, it is at most one time unit before the clock is incremented again, thereby assuming value b_j.

Thus, the total elapsed time until the clock assumes value b_s is $O(s)$. Thereafter, within time $O(\log n)$, the supervisor has received all the needed messages and can deduce that s sessions have occurred and display the "STOP" message. Three time units later, all port processes will have read the "STOP" message and will have stopped performing port events.

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